

Indian Statistical Institute  
Semester-II 2012-2013  
M.Tech.(CS) - First Year  
Class Test I (8 February, 2013)

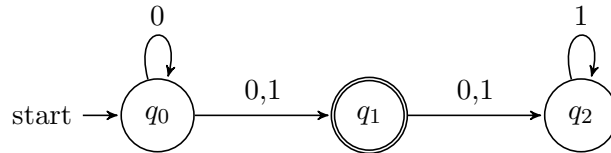
Subject: Automata, Languages and Computation  
Total: 20 marks

To change an answer, scratch out the old answer and write the new answer clearly.  
Do NOT overwrite.

Name: \_\_\_\_\_ Roll: \_\_\_\_\_

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1. Suppose the following non-deterministic finite automaton (NFA) is converted to an equivalent deterministic finite automaton (DFA) using the standard algorithm. [4]



Determine whether each of the following statements is true or false.

- (a)  $\delta(\{q_1\}, 0) = \{q_1, q_2\}$ . TRUE / FALSE  
(b)  $\delta(\{q_2\}, 0) = \{\emptyset\}$ . TRUE / FALSE  
(c) The state  $\{q_0, q_2\}$  is unreachable. TRUE / FALSE  
(d) The state  $\{q_0, q_1, q_2\}$  is a final state. TRUE / FALSE
2. Write down the regular expression for hexadecimal numbers in C. [4]

**Answer:**

3. The language  $L = \{0^p | p \text{ is prime} \}$  is not regular. If you have to prove this using the Pumping Lemma, how many times should you pump  $v$ ? Your answer should be in terms of the lengths of  $u, v, w$  ( $u, v, w$  have their usual significance). [6]

**Answer:**

P.T.O.

4. Let  $M_1 = (Q_1, \Sigma, \delta_1, q_0^{(1)}, F_1)$  and  $M_2 = (Q_2, \Sigma, \delta_2, q_0^{(2)}, F_2)$  be two DFAs. Describe DFAs  $M_{\cup}$  and  $M_{\cap}$  that accept, respectively,  $L(M_1) \cup L(M_2)$  and  $L(M_1) \cap L(M_2)$ . [6]

$M_{\cup}$

$M_{\cap}$

States

\_\_\_\_\_

\_\_\_\_\_

Alphabet

\_\_\_\_\_

\_\_\_\_\_

Transition

\_\_\_\_\_

\_\_\_\_\_

Initial state

\_\_\_\_\_

\_\_\_\_\_

Final states

\_\_\_\_\_

\_\_\_\_\_