



# INDIAN STATISTICAL INSTITUTE

Theoretical Statistics and Mathematics Unit, Kolkata

## SEMINAR

Date: June 13, 2024

Time: 02:00 PM

### VENUE:

**L- 2**

(4<sup>th</sup> Floor, A.N. Kolmogorov Bhavan), ISI Kolkata

### TITLE:

**The Borsuk-Ulam Theorem**

### SPEAKER:

**Kishalay Sarkar**

Stat-Math Unit, ISI Kolkata

### ABSTRACT:

*This seminar will cover the proof of Borsuk-Ulam theorem, which states that, Any odd continuous map from  $S^n$  to  $S^n$  has an odd degree.*

*The proof will use basic aspects of Homology Theory, more specifically Homology with coefficients from the Abelian group  $\mathbb{Z}/2\mathbb{Z}$ . The proof idea involves the construction of a long-exact sequence of homologies (called the transfer sequence) arising out of a 2-sheeted covering triple  $(\tilde{X}, X, p)$ . In particular, the standard 2-sheeted covering  $p: S^n \rightarrow \mathbb{R}P^n$  with the covering map  $p$  sending each  $x \in S^n$  to its antipodal class  $[x] \in \mathbb{R}P^n$ . As a corollary we will derive a useful result which asserts that for any continuous map from  $S^n$  to  $\mathbb{R}^n$ , there is a point  $x_0 \in S^n$  such that  $g(x_0) = g(-x_0)$ .*

**ALL ARE CORDIALLY INVITED**